State selective electron capture in collisions of ground and metastable O\textsuperscript{2+} ions with H(1s).

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Abstract. An ab initio calculation of the electron capture cross sections for collisions of ground and metastable states of O\textsuperscript{2+} with H(1s) is presented. For impact energies between 0.125 and 3.4 keV/amu, we find good agreement between the cross sections from the ground state ion with the mixed beam experimental data of Phaneuf et al (1982).

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1. Introduction

Electron capture (EC) in ion–atom(molecule) collisions are important processes in astrophysical and fusion plasmas. However, the measurement of cross sections for these processes is often difficult due to the presence of unknown quantities of metastable species in the ion beam. Examples of this difficulty are C\textsuperscript{2+} collisions with H, He, and H\textsubscript{2}, which have been considered in several theoretical and experimental works (Unterreiter et al 1991, Castillo et al 1994, Leputsch et al 1997, Voulot et al 2000, Errea et al 2000a, Errea et al 2000b). Recently, double translational energy techniques have allowed to measure EC cross sections for ions in both ground and metastable states (see, e.g. the data for C\textsuperscript{2+} + H and N\textsuperscript{2+} + H collisions of Voulot et al (2000) and Voulot et al (2001)). Similarly, O\textsuperscript{2+} beams from usual ion sources are, in principle, a mixture of unknown proportions of ground state (1s\textsuperscript{2}s\textsuperscript{2}s\textsuperscript{2}p\textsuperscript{2} \textsuperscript{3}P) and metastable (1s\textsuperscript{2}s\textsuperscript{2}s\textsuperscript{2}p\textsuperscript{2} \textsuperscript{1}D and 1s\textsuperscript{2}s\textsuperscript{2}s\textsuperscript{2}p\textsuperscript{2} \textsuperscript{1}S) ions, and accordingly, the following EC reactions can take place in O\textsuperscript{2+} + H experiments:

\begin{align*}
O\textsuperscript{2+}(1s^22s^22p^2 \textsuperscript{3}P) + H(1s) & \rightarrow O^+ + H^+ \quad (1) \\
O\textsuperscript{2+}(1s^22s^22p^2 \textsuperscript{1}D) + H(1s) & \rightarrow O^+ + H^+ \quad (2) \\
O\textsuperscript{2+}(1s^22s^22p^2 \textsuperscript{1}S) + H(1s) & \rightarrow O^+ + H^+ \quad (3)
\end{align*}

Experimental works on this system include the measurements of EC cross sections of Phaneuf et al (1982), carried out with a mixed beam. McLaughlin et al (1990) measured

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EC energy change spectra for impact energies in the range 0.125–0.5 keV/amu using also a mixed beam; the recorded spectra show two peaks, one at $\Delta E \approx 6.5$ eV and a second at 3.5 eV; this second peak was assigned to capture by metastable ions. The use of double translational energy spectroscopy technique allowed to record the energy change spectrum for EC at a collision energy of 0.375 keV/amu and for an incident pure beam of ground state ions (McCullough 2000), which showed a single peak at $\Delta E \approx 6.5$ eV corresponding to EC into $\text{O}^+(1s^22s^22p^4\,^4\text{P})$. EC cross sections have not been measured with pure beams and state selective experimental cross sections have not been reported hitherto.

From the theoretical point of view, the calculation of EC cross sections at low impact energies is carried out by employing a molecular expansion, which involves the previous evaluation of potential energy surfaces and dynamical couplings of the corresponding quasimolecule. For many-electron systems, this calculation requires the adaptation of quantum chemistry packages. In particular, for collisions involving metastable species, several initial states must be considered, and one has to include a relatively large number of molecular states, which must be evaluated with the same precision in a wide range of internuclear separations; this is a non standard task for those packages, and their application to dynamical problems have been considered in previous works (Castillo et al 1994, Castillo et al 1995, Errea et al 2000b).

Honvault et al (1994) evaluated total cross sections for reactions (1–3) at a range of energies from 1.25 eV/amu to 1.87 keV/amu. The molecular energy curves and couplings were evaluated by using a SCF-CI technique, where the ground state is, in general, described more precisely than the excited states. The results from that calculation suggested that a relatively high proportion (60%) of metastable ions was present in the experiment of Phaneuf et al (1982). Given the sensitivity of the cross sections to the quality of the molecular data, and in order to evaluate state-selective EC cross sections, we have carried out an extensive molecular calculation using the techniques previously applied to $\text{C}^2++\text{H}, \text{H}_2$ collisions (Errea et al 1999, Errea et al 2000b, Errea et al 2000a).

Our dynamical calculations have been carried out by applying a method similar to that of Errea et al (2000a), which is described in section 2. We employ a semiclassical treatment with a close-coupling molecular expansion, where the electronic energies and non-adiabatic couplings for doublet and quadruplet states of the $\text{OH}^2+$ quasimolecule are obtained in a multireference configuration interaction calculation. The details of the molecular calculation are presented in section 3 and the dynamical calculations in section 4. Our main conclusions are outlined in section 5. Atomic units are used unless otherwise indicated.

2. Method

For not too low impact energies ($E \gtrsim 50$ eV/amu), the dynamics of ion-atom collisions is usually treated using the impact-parameter method (see e.g. Bransden and McDowell (1992)), where the nuclear motion follows straight-line trajectories with constant velocity
and impact parameter $b$ ($\mathbf{R} = \mathbf{b} + \mathbf{v}t$), while the electronic motion is described by the wavefunction $\Psi(\mathbf{r}, t; b, v)$, solution of the equation

$$
\left( H_{\text{elec}} - i \frac{\partial}{\partial t} \right) \Psi(\mathbf{r}, t; b, v) = 0
$$

(4)

where $H_{\text{elec}}(\mathbf{r}; R)$ is the non-relativistic, clamped-nuclei Born-Oppenheimer electronic Hamiltonian, and $\mathbf{r}$ denotes the electronic coordinates. If $n_A$ and $n_B$ are the number of electrons initially attached to nucleus A and B, respectively, the semiclassical equation (4) must be solved with the initial condition:

$$
\Psi(\mathbf{r}, t; b, v) \sim \Phi_i^A \Phi_i^B \prod_{j=1}^{n_A} D^A(\mathbf{r}_j) \prod_{j'=1}^{n_B} D^B(\mathbf{r}_{n_A+j'}) \exp \left[ -i(E_i^A + E_i^B)t \right],
$$

(5)

where $\Phi_i^{A,B}$ are atomic wavefunctions with energies $E_i^{A,B}$, and $D^{A,B}$ are plane-wave translation factors, which describe the translation motion of the electrons attached to each nucleus:

$$
D^X(\mathbf{r}_j) = \exp \left[ -i(\mathbf{v}_X \cdot \mathbf{r}_j + \frac{1}{2} \mathbf{v}_X^2 t) \right]; \quad (X = A, B)
$$

(6)

where $\mathbf{v}_{A,B}$ are the nuclear velocities with respect to the electronic coordinates origin, placed at an arbitrary point of the internuclear axis.

Analogously to equation (5), the wavefunction for a collisional final state is:

$$
\psi_f(\mathbf{r}, t; b, v) = \Phi_f^A \Phi_f^B \prod_{j=1}^{n'_A} D^A(\mathbf{r}_j) \prod_{j'=1}^{n'_B} D^B(\mathbf{r}_{n'_A+j'}) \exp \left[ -i(E_f^A + E_f^B + \alpha_f)t \right],
$$

(7)

where $|n'_A - n_A|$ is the number of electrons that have been exchanged and $\alpha_f = Q_A Q_B v^{-1} \log(R - vt)$ comes from the Coulomb interaction between the two ions with charges $Q_{A,B}$ formed in the collision.

To solve equation (4), $\Psi$ is expanded in a set of (approximate) eigenfunctions $\phi_k$ of $H_{\text{elec}}$:

$$
\Psi(\mathbf{r}, t; b, v) = \exp(iU) \sum_k a_k(t; b, v) \phi_k(\mathbf{r}; R) \exp \left( -i \int_{-\infty}^{t} \epsilon_k dt' \right)
$$

(8)

where

$$
H_{\text{elec}}(\mathbf{r}; R) \phi_k(\mathbf{r}; R) = \epsilon_k(R) \phi_k(\mathbf{r}; R)
$$

(9)

and $\exp[iU(\mathbf{r}, t)]$ is a common translation factor (Schneiderman and Russek 1969). Our translation factor has the form (see Errea et al (1994)):

$$
U(\mathbf{r}, t) = \sum_{j=1}^{n_A+n_B} \left[ f(\mathbf{r}_j, R) \mathbf{v} \cdot \mathbf{r}_j - \frac{1}{2} f^2(\mathbf{r}_j, R) v^2 t \right]
$$

(10)

with (Errea et al 1982):

$$
f(\mathbf{r}_j, R) = g(R) \mathbf{r}_j \cdot \mathbf{R} = \frac{R}{R^2 + \beta^2} \mathbf{r}_j \cdot \mathbf{R}.
$$

(11)
In the present calculation, the switching function $f$ has been defined with $\beta = 2$ and with the coordinates $r_j$ referred to the O nucleus. Substitution of equation (8) in (4) leads to the system of differential equations:

$$i\dot{a}_k = \sum_l M_{kl}a_l \exp \left[ -i \int_{-\infty}^{t} (\epsilon_l - \epsilon_k) dt' \right],$$

where $M_{kl}(R; b, v)$ are the non-adiabatic couplings:

$$M_{kl} = \left\langle \exp(iU)\phi_k \right| H_{\text{elec}} - i\frac{\partial}{\partial t} \left\langle \exp(iU)\phi_l \right|$$

In the energy range of this work, the transitions between the molecular states are mainly due to the components of $M_{kl}$ proportional to $v$, which have the form:

$$\frac{v^2}{R}R_{kl} + \frac{bv}{R^2}L_{kl}$$

and, by analogy with the molecular expansion without translation factors, $R_{kl}$ and $L_{kl}$ are known as modified radial and rotational couplings, respectively. For the translation factor of equations (10) and (11), they are:

$$R_{kl} = \left\langle \phi_k \left| \frac{\partial}{\partial R} + \sum_j \left[ (Rg^2 - 2g)z_j \frac{\partial}{\partial z_j} \right] \phi_l \right| \rightangle$$

and

$$L_{kl} = \left\langle \phi_k \left| \sum_j \left[ iL_y(r_j) - gR \left( x_j \frac{\partial}{\partial z_j} + z_j \frac{\partial}{\partial x_j} \right) \right] \phi_l \right| \rightangle$$

where $L_y$ is the Y component of the electronic angular momentum operator, and $x_j, z_j$ are the electronic coordinates in the molecular reference frame.

The probability for transition to the final state $\psi_f$ is calculated from the coefficient $a_f$ of equation (8)

$$P_f(b, v) = \lim_{t \to \infty} |\langle \psi_f |\Psi \rangle - \delta_{ij}|^2 = \lim_{t \to \infty} |a_f(t; b, v) - \delta_{ij}|^2,$$

and the total cross section for transition to this state is:

$$\sigma_f(v) = 2\pi \int_0^\infty \sigma_f(b, v) \, db.$$

### 3. Molecular calculations

Since the entrance channel of reaction (1) correlates to quadruplet and doublet molecular states, and those of reactions (2) and (3) correlate with doublet states, we have calculated doublet and quadruplet states of the OH^{2+} quasimolecule.

The molecular states $\phi_j$ and energies $\epsilon_j$ were obtained by using a multireference configuration interaction method (MRCI) with the program MELD (Davidson 1990). This method involves, in a first step, a SCF calculation in a basis of Gaussian type orbitals (GTOs), which provides a set of molecular orbitals (MOs). A set of reference
configurations is then selected. Each reference configuration is a symmetry- and spin-
adapted linear combination of a few Slater determinants built up from products of the
MOs. The configuration interaction (CI) space includes single and double excitations
from the reference set.

In the present calculation, the GTO basis sets, centered at the O and H nuclei,
were taken from Widmark et al (1990) and consist in \{4s,3p,2d\} and \{3s,2p\} contracted
GTOs, respectively. The MOs were obtained in a restricted SCF calculation of the
OH$^{5+}$ system. In this case, in the limit $R \to \infty$, the SCF configuration correlates to the
1s$^2$2s$^2$ configuration of O$^{4+}$, so the 2p$_x$ and 2p$_y$ orbitals, both unoccupied, have the same
coefficients. This allows to describe, with the same accuracy, the states involved in the
collisional system (see table 1). We have checked that the calculated molecular energies
do not significantly change when the CI calculation is carried out with MOs obtained
in a SCF calculation for the OH$^{7+}$ quasimolecule. The CI space was built from a set
of 160 reference configurations, but, to obtain a reasonable size of this space, we have
introduced the following restrictions: i) Frozen core approximation, which means that
we keep only configurations with the ground MO, 1\sigma, doubly occupied. ii) Second order
perturbation theory is used to select doubly excited configurations. In this selection, our
zeroth order wavefunctions are the eigenvectors of the Hamiltonian matrix in the basis
of reference configurations, and we have included configurations with a contribution to
the energy of the first 18 quadruplet and 27 doublet states greater than 5 \times 10^{-6} Hartree.

The set of reference configurations was selected iteratively at each $R$ in the following
way: An initial guess of 160 reference configurations was generated in the limit $R \to \infty$,
which contained the basic structures of the atomic channels to be included in the
dynamical calculation (those listed in table 1). Using this set we carried out a MRCI
calculation, and we selected the 160 configurations with the largest contributions to the
lowest 18 (quadruplets) and 27 (doublets) states obtained in this calculation, which were
then used as a new reference set and the selection procedure was repeated. After three
iterations the reference set has converged and the weight of the reference configurations
in the calculated CI functions is larger than 95% for the states of table 1. To ensure
a similar precision of wavefunctions at any internuclear distance, the selection of the
reference set was repeated at each value of $R$, with the converged reference set at a
given value of the internuclear distance, $R_i$, used as the initial guess in a nearby point
$R_{i+1}$ ($R_i > R_{i+1}$). In practice, $R_i - R_{i+1} = 0.2 \text{ a}_o$ except for $R < 4 \text{ a}_o$ and in the
region of avoided crossings at 8.5–9.3 \text{ a}_o, where the stepsizes was reduced to 0.05 \text{ a}_o.
The CI space included about 20000 Slater determinants for each multiplicity, while the
calculation of Honvault et al (1994) included less than 400.

As a check of the accuracy of our calculation, we compare in table 1 the calculated
energies of the O$^+$ and O$^{2+}$ states included in the dynamical calculation with the
experimental values of Moore (1971). The tabulated energies are relative to the ground
state of O$^{2+}$. The errors in these energy differences are smaller than 0.5 eV for the
relevant channels, sufficient for the dynamical calculation. Also included in the table
are the corresponding molecular states of OH$^{2+}$.
The entrance channels for reaction (1) are the molecular states $1^3\Sigma^+$ and $6$ in the avoided crossings at $R$ (see figure 3a). These transitions are strongly modified by the rotational transitions induced by the rotational couplings (see equation (15)) and in figure 4 some rotational ones (equation (16)). The meaning of the dynamical couplings. To solve this arbitrariness, we have implemented an algorithm to automate the sign coherence of the molecular states.

As an illustration, we have plotted in figure 3 the most important modified radial couplings (see equation (13)) and in figure 4 some rotational ones (equation (16)). The main mechanism of reaction (1) involves transitions in the neighborhood of $1^4\Sigma^+ - 5^4\Sigma^-$ (at $R \approx 4.0$ and $3.5 \, \text{a}_0$) and $1^4\Pi - 5^4\Pi$ (at $R \approx 4.5$ and $2.5 \, \text{a}_0$) avoided crossings in figure 1, which are responsible for the two-peak structure of the corresponding couplings in figure 3a. These transitions are strongly modified by the rotational transitions induced by $1^4\Sigma - 1^4\Pi$ and $5^4\Sigma - 5^4\Pi$ rotational couplings of figure 4a.

Reaction (2) takes place through transitions between states of the multiplets 2 (the entrance channels) and 6 in the avoided crossings at $R$ in the range 2–3 $\text{a}_0$ (see figure 3b). Also, in the range of impact energies of this work, small transitions take place in the sharp avoided crossings at $R \approx 8.8 \, \text{a}_0$ (figure 3c), which are crossed almost diabatically.
However, these transitions cannot be neglected in the calculation of cross sections for reaction (2) because of the large internuclear distances involved. The energy of the molecular state $^3\Sigma^+$, which is the entrance channel of reaction (3), shows avoided crossings with that of state $^2\Sigma^+$ at $R \simeq 4.8$ and 2.5 a.u. The most important transitions leading to reaction (3) are due to the radial couplings between the entrance channel and states 2 and 9$^2\Sigma^+$ plotted in figure 3d.

4. Results

Our calculated total cross sections for reactions (1)–(3) are listed in table 2 and plotted in figure 5, where we have also included the contribution of the quadruplets states to the cross section of reaction (1) to show that this process is dominated by the quadruplet subsystem. In figure 6, we plot the contribution ratio of the individual channels, calculated as

$$k_i = \frac{\sigma_i}{\sum_j \sigma_j}.$$
with $i$ and $j$ running over the EC channel index.

At low energies (below 1.25 keV/amu), the EC process (1) involves the capture of the target electron into the 2p orbital with simultaneous excitation of a 2s electron to the 2p orbital (exit channels 5 and 6 of table 1). This result agrees with the translation energy spectra of McLaughlin et al. (1990) and McCullough (2000) which exhibit a single peak for reaction (1) at $E < 0.5$ keV/amu. At higher energies, the capture into the 3s orbital (channels 7 and 8) becomes competitive with the previous process, and these transitions are responsible for the increase of the total cross section in figure 5 for $E > 1.25$ keV/amu.

Reaction (2) takes place through transitions in the avoided crossings $2^2\Sigma^+-6^2\Sigma^+$, $2^2\Pi-6^2\Pi$ and $2^2\Delta-6^2\Delta$, which explains that O$^+$(2D) is the most abundant product of this reaction. O$^+$(2S) is a secondary output of this process with a contribution rising up to 10% at 1.25 keV/amu (see figure 6); this channel is populated through a two-step mechanism $6^2\Sigma-3^2\Sigma-9^2\Sigma$. Again, our results are consistent with translation energy spectra of McLaughlin et al. (1990), which show a second peak at $\Delta E \approx 3.4$ eV.
Figure 3. Selected radial couplings between terms of different channels, as indicated in the panels.

Figure 4. Selected rotational couplings between terms of different channels, as indicated in the panels.
Table 2. Electron capture cross sections (in Å²) for reactions (1), (2) and (3).

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that can be ascribed to the formation of O⁺(2D) in reaction (2). The total EC cross section for O²⁺(1D)+H collisions (figure 5) is practically constant because, at relatively high v, the depopulation of individual states through rotational couplings increases the effectiveness of transitions in the avoided crossings 2{2Σ⁺, 2Π, 2Δ}–6{2Σ⁺, 2Π, 2Δ}. On the other hand, the EC mechanism in O²⁺(1S)+H collisions involves, mainly, transitions from the entrance channel (3²Σ⁺) to states 2²Σ⁺ (and from this to 6²Σ⁺, in last part of the collision) and 9²Σ⁺ (see the corresponding couplings in figure 3d). The 3²Σ⁺–2²Σ⁺ avoided crossing at R ≈ 5 a₀ is traversed diabatically when v increases, which explains the decrease of the total cross section for reaction (3) in figure 5. For E ≥ 1 keV/amu, 3²Σ⁺–9²Σ⁺ transitions become more important, giving rise to the increase of the partial cross section for formation of O⁺(2S) (see figure 6c).

We obtain good agreement between our theoretical EC cross sections from O²⁺ (3P) ions with experimental data of Phaneuf et al (1982), and worse agreement is found by assuming a contamination of the initial beam by metastable O²⁺(1D) or O²⁺(1S) ions. Therefore, our results indicate that there was not beam contamination in the experiment of Phaneuf et al (1982). In practice, although the order of magnitude of the total cross for reaction (1) of Honvault et al (1994) is similar to ours, it does not reproduce the decrease of the experimental cross section for E ≥ 0.45 keV/amu, because of the limitations of their molecular calculation, and lead them to suggest a high proportion of metastable ions in the initial beam.

5. Conclusions

We have calculated the state selected EC cross sections in collisions of O²⁺ with H(1s), for various initial states of O²⁺, by employing a molecular expansion with ab initio molecular wavefunctions evaluated with a MRCI technique. The cross sections for EC by
Figure 5. Total electron capture cross sections in O$^{2+}$+H(1s) collisions from various O$^{2+}$ initial states, as labeled in the figure. In the case of O$^{2+}$($^{3}$P)+H(1s) collisions, the quadruplets contribution is indicated. Symbols are experimental values from (Phaneuf et al 1982).

ground state O$^{2+}$ ions are in agreement with previous experimental data of Phaneuf et al (1982). We have calculated the branching ratio for populating different EC channels and we show that electron capture with simultaneous projectile excitation is the preferred channel at energies below 1.25 keV/amu, while the direct capture to the 3s orbital of O$^{+}$ starts to be competitive at $E \gtrsim 1.25$ keV/amu. O$^{+}$ (2s2p$^4$ 2D) is practically the only product of capture from O$^{2+}$($^{1}$D), while O$^{+}$ (2s2p$^4$ 2D) and O$^{+}$ (2s2p$^4$ 2S) are obtained from O$^{2+}$($^{1}$S).
$O^{2+} + H$ collisions

![Graphs showing branching ratio to electron capture channels in $O^{2+} + H(1s)$ collisions. Products are indicated in the panels. Panel (a) is for $O^{2+}(^3P) + H(1s)$, panel (b) for $O^{2+}(^1D) + H(1s)$ and panel (c) for $O^{2+}(^1S) + H(1s)$.](image)

**Figure 6.** Branching ratio to electron capture channels in $O^{2+} + H(1s)$ collisions. Products are indicated in the panels. Panel (a) is for $O^{2+}(^3P) + H(1s)$, panel (b) for $O^{2+}(^1D) + H(1s)$ and panel (c) for $O^{2+}(^1S) + H(1s)$.

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**References**


$O^2+ + H$ collisions


McCullough R W 2000 Unpublished results


